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MODELING IN  
ASTROPHYSICS

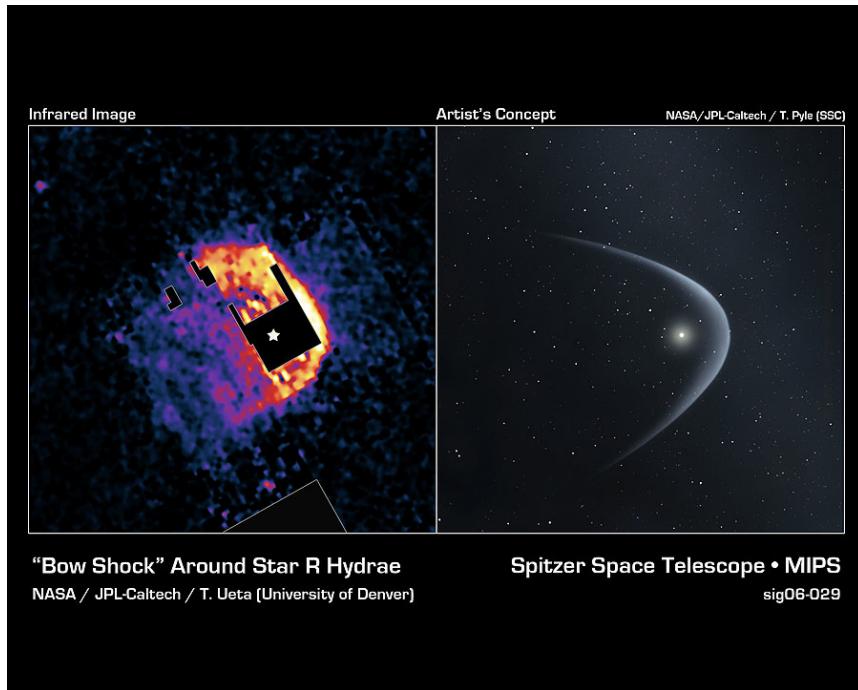
# Charge Exchange in the Colliding Winds of Hot Jupiters and Their Host Stars

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# Example of colliding winds

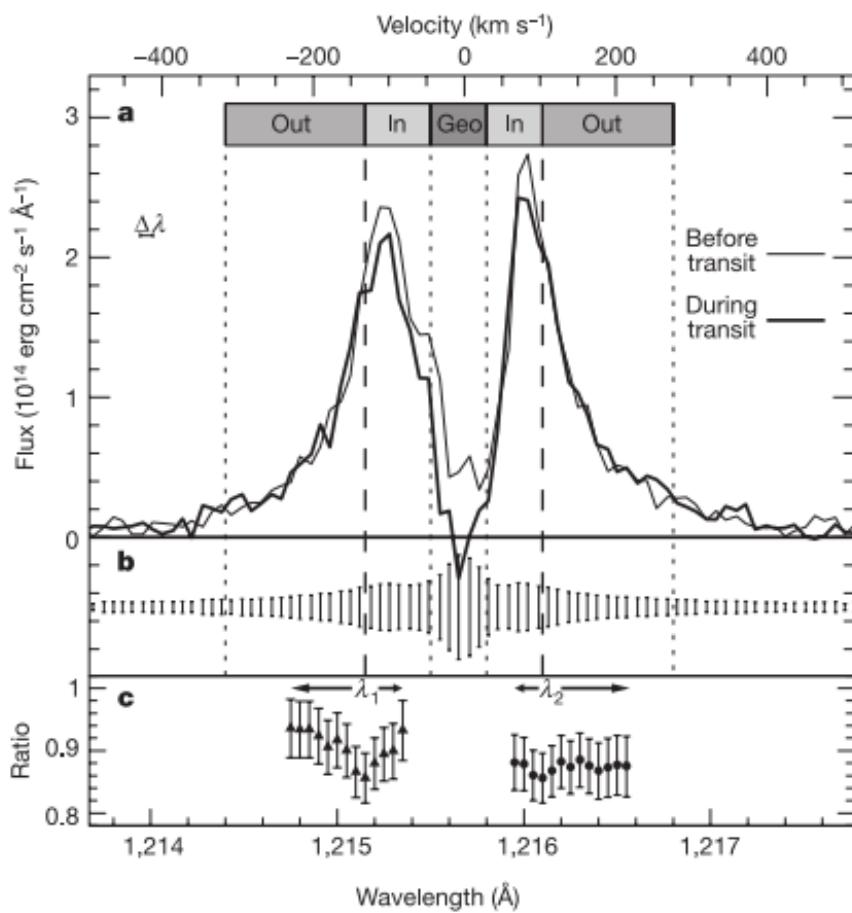
- Massive star winds in binaries
- Stellar wind on the atmospheric escape of an hot jupiter
- Stellar winds on the interstellar medium
- Solar wind on the Earth magnetosphere



- AGB Star R Hydriae in the far infrared

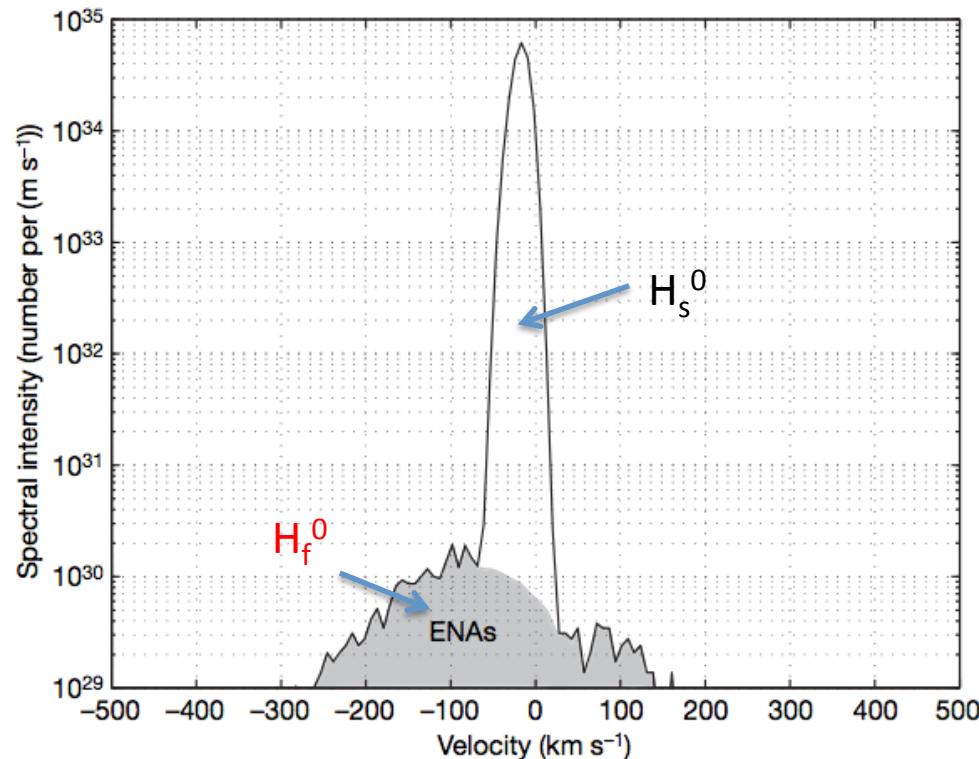
*Ueta et al 2006*

# Atmospheric escape: HD209458b



- *Vidal-Madjar et al. 2003*
  - ~10% absorption of the stellar Ly $\alpha$  spectrum
  - Absorption at high velocities (+/- 100 km/s)

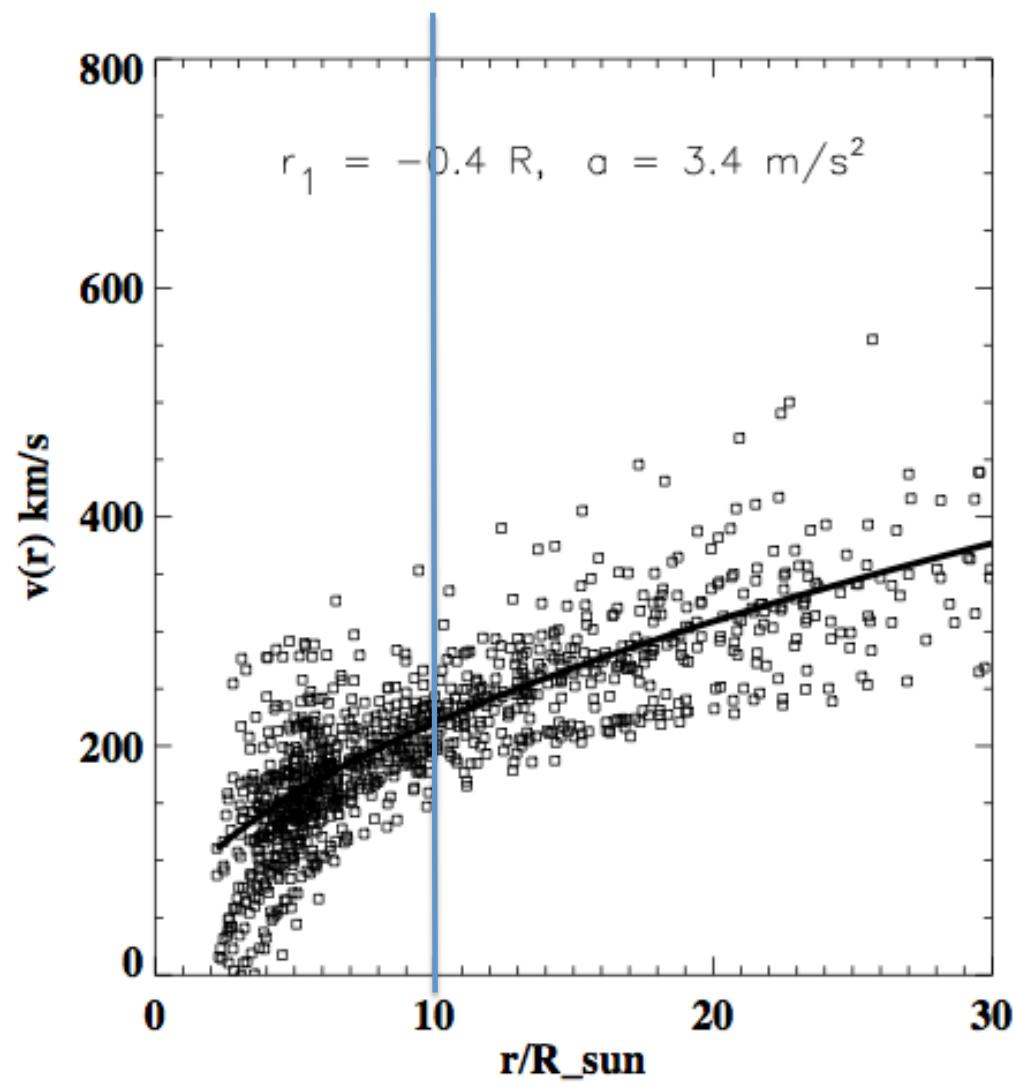
# Charge exchange: HD209458b



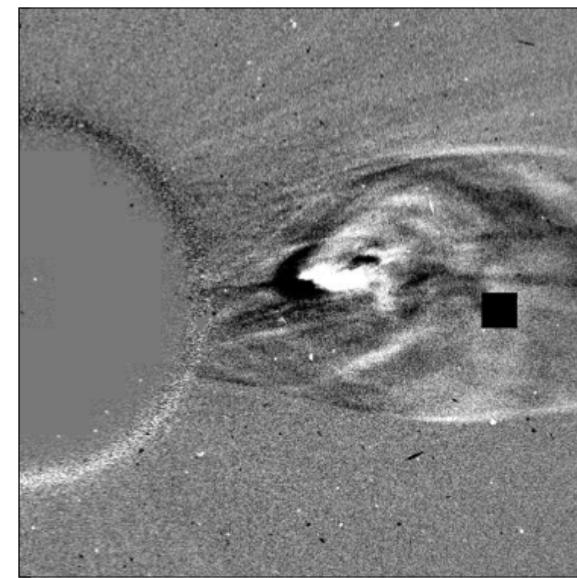
- *Holmström et al. 2008*
  - Charge exchange processes
  - $H_f^+ + H_s^0 \rightarrow H_s^+ + H_f^0$
- $H_f^+$ : Fast ionized hydrogen in the solar wind
- $H_s^0$ : Slow neutral hydrogen in the planetary wind
- $H_f^0$ : Fast neutral hydrogen in the mixing layer

➤ But assume no shocks and a subsonic solar wind at 50 km/s

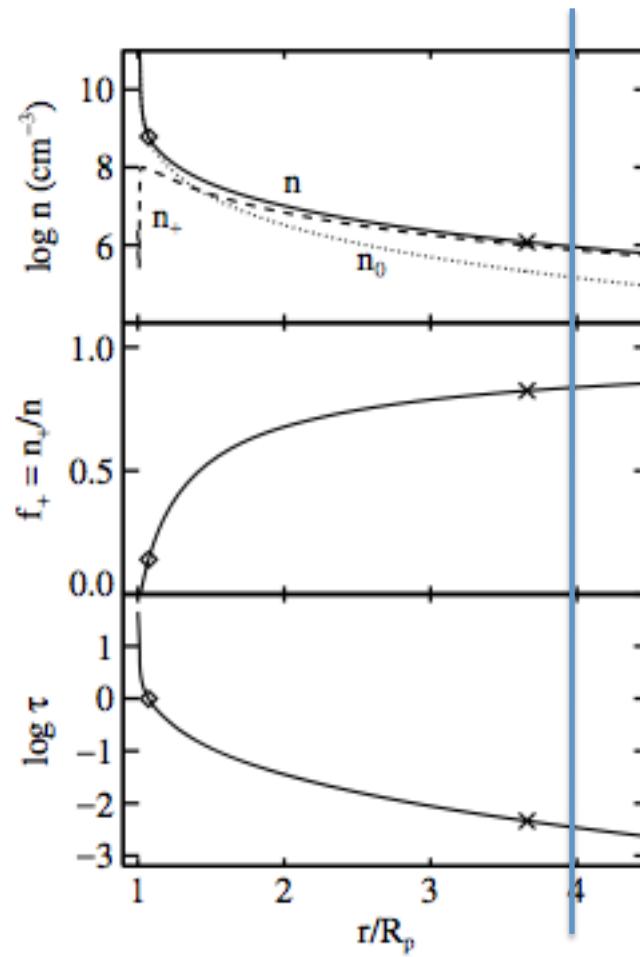
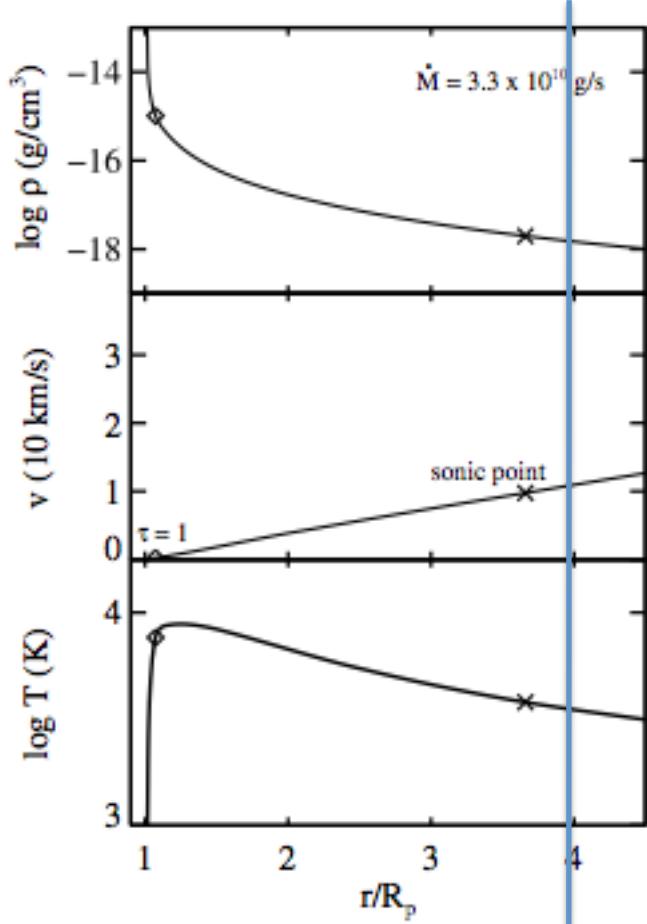
# Solar wind: Data and Parker solution



- *Sheeley et al 1997*
- At  $r = 10 R_\odot$  (0.05 au):
  - $n_* = 2000/\text{cm}^3$
  - $T_* = 10^6 K$
  - $v_* = 250 \text{ km/s}$
  - $f_*^+ = 1$
  - $c_* = 130 \text{ km/s}$
  - $M_* \approx 2$



# Planetary wind model



At  $r = 4 R_p$ :

$$\begin{aligned} n_p &= 10^6 \text{ cm}^{-3} \\ T_p &= 7000 K \\ v_p &= 10 \text{ km/s} \\ f_p^+ &= 0.8 \\ c_p &= 11 \text{ km/s} \\ M_p &\approx 1 \end{aligned}$$

- Murray-Clay et al. 2009
  - Standard planetary wind model driven by the stellar UV flux

# Cooling processes

Solar wind:

- Thermal conductivity (*Spitzer 1953*)

$$- K \approx 1.7 \times 10^4 (T/T_6)^{5/2} \quad [W/m/K]$$

$$- D = K/\rho_* c \approx 4 \times 10^{21} \quad [cm^2/s]$$

$$- t_{cool} \approx R_p^2/D \approx 2 \times 10^{-2} s$$

- Hydrodynamic timescale:

$$t_{hd} \approx R_*/v_* \approx 4 \times 10^4 s$$

$$\rightarrow t_{cool} \ll t_{hd}$$

- Isothermal solar wind at  $T = 10^6$  K

Planetary wind:

- Lyα cooling rate at 7000 K

$$\Lambda \approx 2 \times 10^{-18} cm^3 erg/s$$

$$t_{cool} \approx e_p/(n_p^2 \Lambda) \approx 20 s$$

- Hydrodynamic timescale:

$$t_{hd} \approx R_*/v_p \approx 4 \times 10^5 s$$

$$\rightarrow t_{cool} \ll t_{hd}$$

- Isothermal planetary wind at  $T = 7000$  K
- Simulations with  $\gamma = 1.01$

# Neglected effects

- Magnetic field *Weber & Davis 1967*

At  $r = 0.05$  au (10  $R_*$ ):

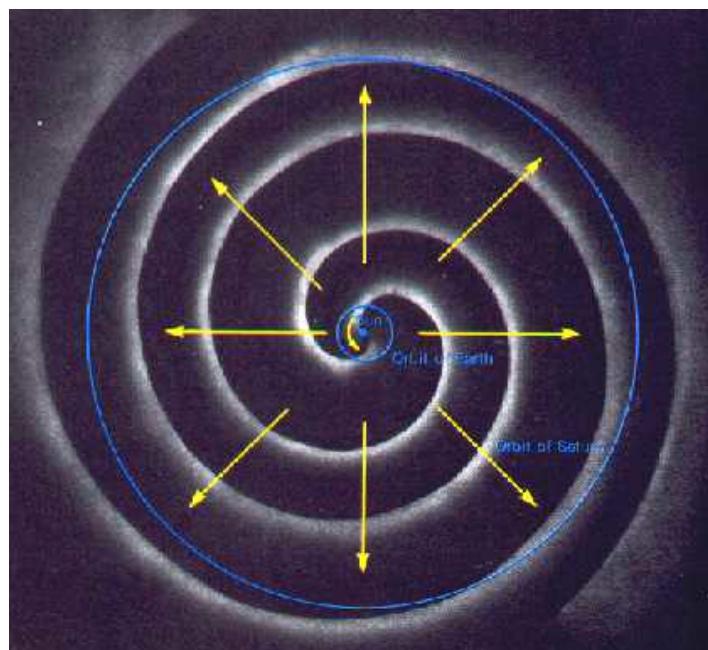
$$B_r \approx 0.1G \quad B_\phi \approx 4 \times 10^{-4}G$$

$$\beta_\phi \approx 157$$

- Coriolis force

$$a \approx 2\Omega v_p \quad \Delta v \approx 2\Omega R_*$$

➤  $\Delta v \approx 20\text{ km/s}$

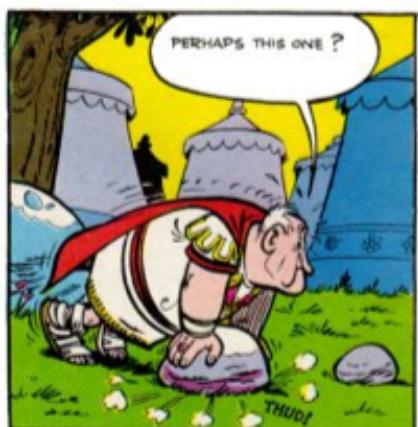




- 3D simulations



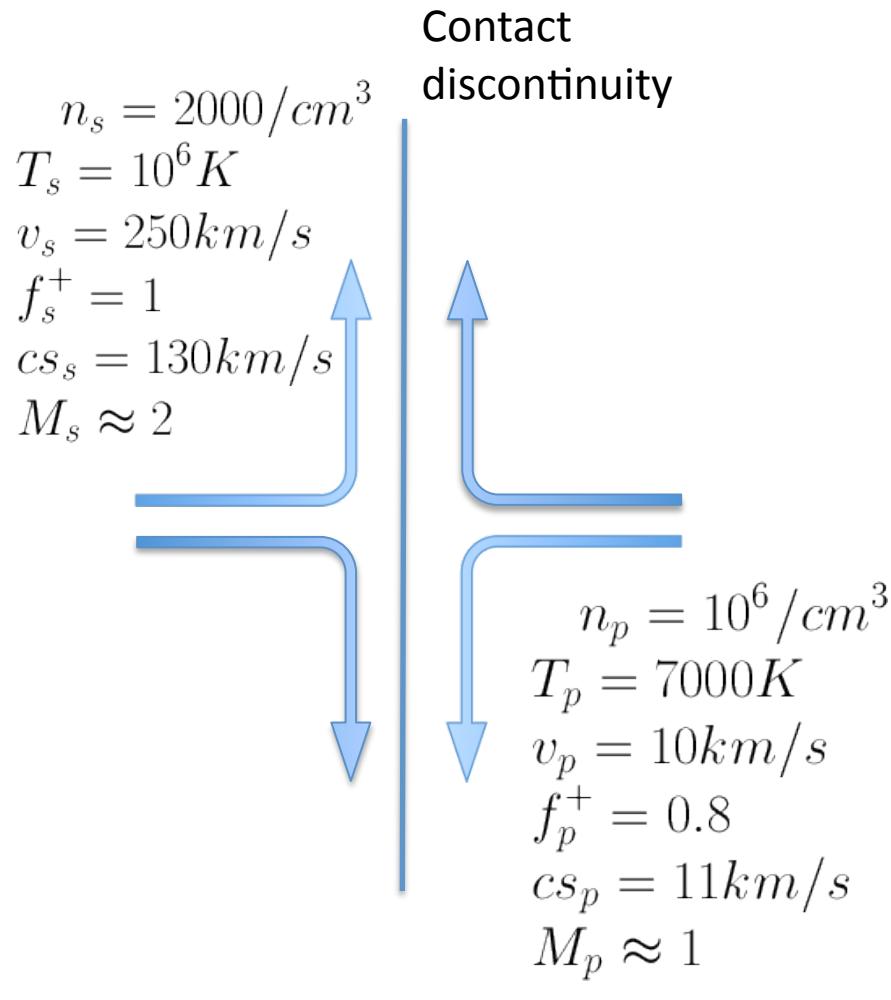
- 2D simulations



- Semi-analytic solution for bow shocks

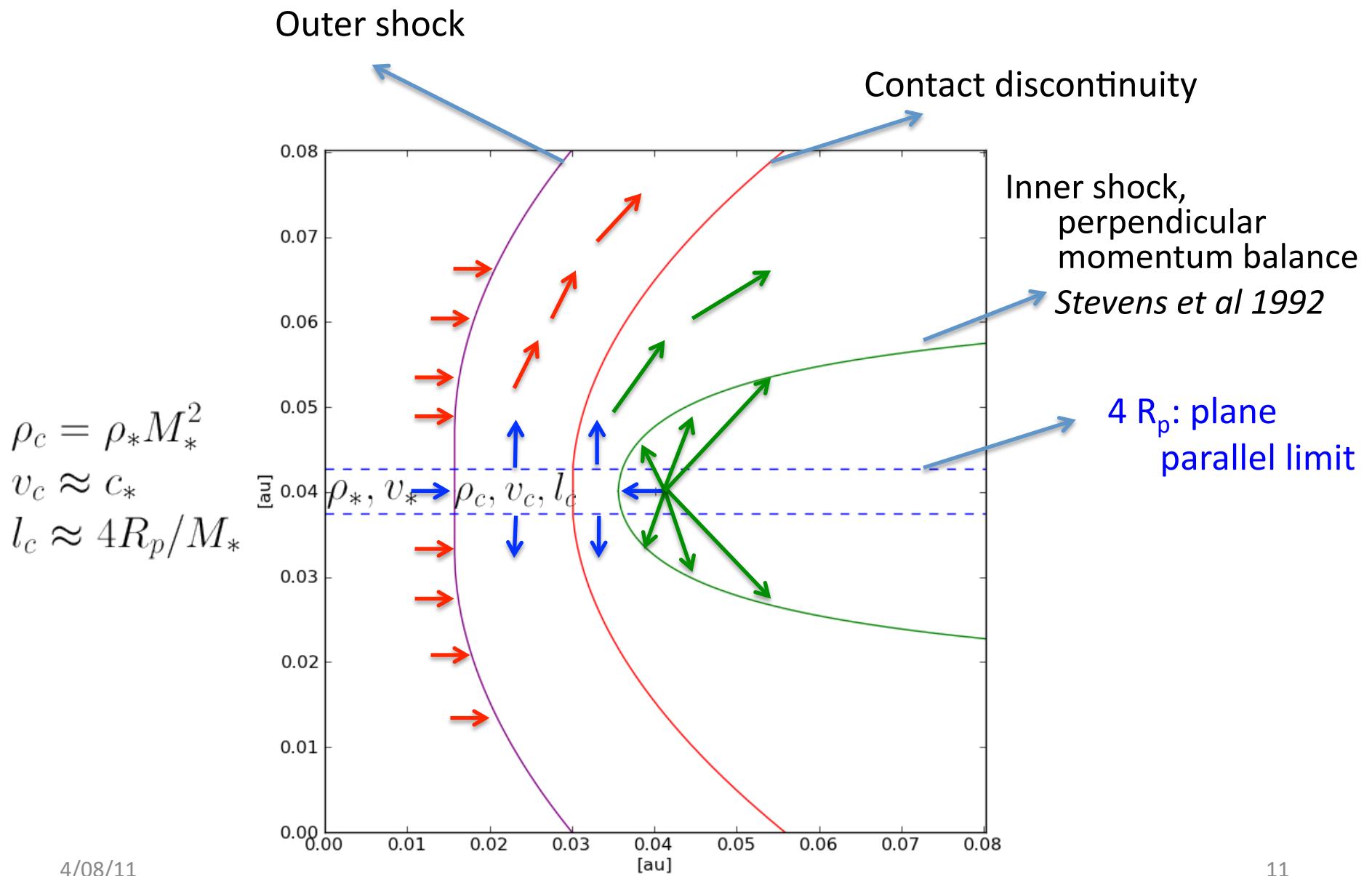
- Plan-parallel order of magnitude estimation

# Order of magnitude estimation



- Mixing by Kelvin Helmholtz instabilities  
 $v_{mix}, t_{mix}, l_{mix}$
- Charge exchange cross section:  
 $\sigma_{ce} \approx 2 \times 10^{-15} cm^2$
- Ly $\alpha$  opacity at line centre:  
 $\tau \approx 3.31 \times 10^{-14} T_4^{-0.5} N_{H^0}$
- Estimations:  
 $N_{H_f^0} \approx 10^{15}/cm^2$   
 $\tau \approx 3$

# 2D structure of the interface

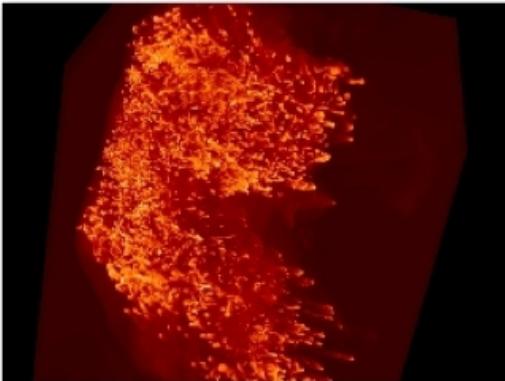


# 2D/3D simulations, HERACLES

## HERACLES

3D parallel code for hydrodynamics, MHD, radiative transfer and gravity

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**HERACLES** is a 3D hydrodynamical code used to simulate astrophysical fluid flows. It uses a finite volume method on fixed grids to solve the equations of hydrodynamics, MHD, radiative transfer and gravity. This software is developed at the [Service d'Astrophysique, CEA/Saclay](#) as part of the [COAST project](#) and is registered under the [CeCILL](#) license.

The code is developed by:

- Code architecture: Edouard Audit
- Parallelization: Edouard Audit
- Hydrodynamics: Edouard Audit
- Radiative transfer: Matthias González, Edouard Audit & Neil Vaytet
- MHD: Sébastien Fromang, Patrick Hennebelle & Romain Teyssier
- Gravity: Pascal Tremblin
- HDF5 output: Bruno Thooris
- Website: Neil Vaytet

HERACLES simulates **astrophysical fluid flows** using a grid based Eulerian finite volume Godunov method. It is capable of simulating **pure hydrodynamical** flows, **magneto-hydrodynamic** flows, **radiation hydrodynamic** flows (using either flux limited diffusion or the M1 moment method), **self-gravitating** flows using a Poisson solver or all of the above. HERACLES uses cartesian, spherical and cylindrical grids. Current ongoing developments include a **multi-grid** method and a **multi-group** scheme for the radiative transfer.

The full package can be downloaded here: [heracles.tar.gz](#)  
Current version: 2.0 (20 September 2010)  
[Version history](#)

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COAST project home page - Service d'Astrophysique, CEA/SAp



# 2D/3D simulations, Charge exchange

- Passive scalars advected to the flow

$$\frac{\partial x_f^+ \rho}{\partial t} + \nabla \cdot (u x_f^+ \rho) = 0$$

$x_f^+ = 1$  in solar wind

$$\frac{\partial x_s^0 \rho}{\partial t} + \nabla \cdot (u x_s^0 \rho) = 0$$

$x_s^0 = 0.2$  in planetary wind

- Charge exchange process  $H_f^+ + H_s^0 \rightarrow H_s^+ + H_f^0$

$$dx_f^+ n_H / dt = -\sigma_{ce} x_f^+ x_s^0 n_H^2 v_{th}$$

$$dx_s^0 n_H / dt = -\sigma_{ce} x_f^+ x_s^0 n_H^2 v_{th}$$

$$dx_f^0 n_H / dt = \sigma_{ce} x_f^+ x_s^0 n_H^2 v_{th}$$

# 2D simulation, post processing Ly $\alpha$ spectra

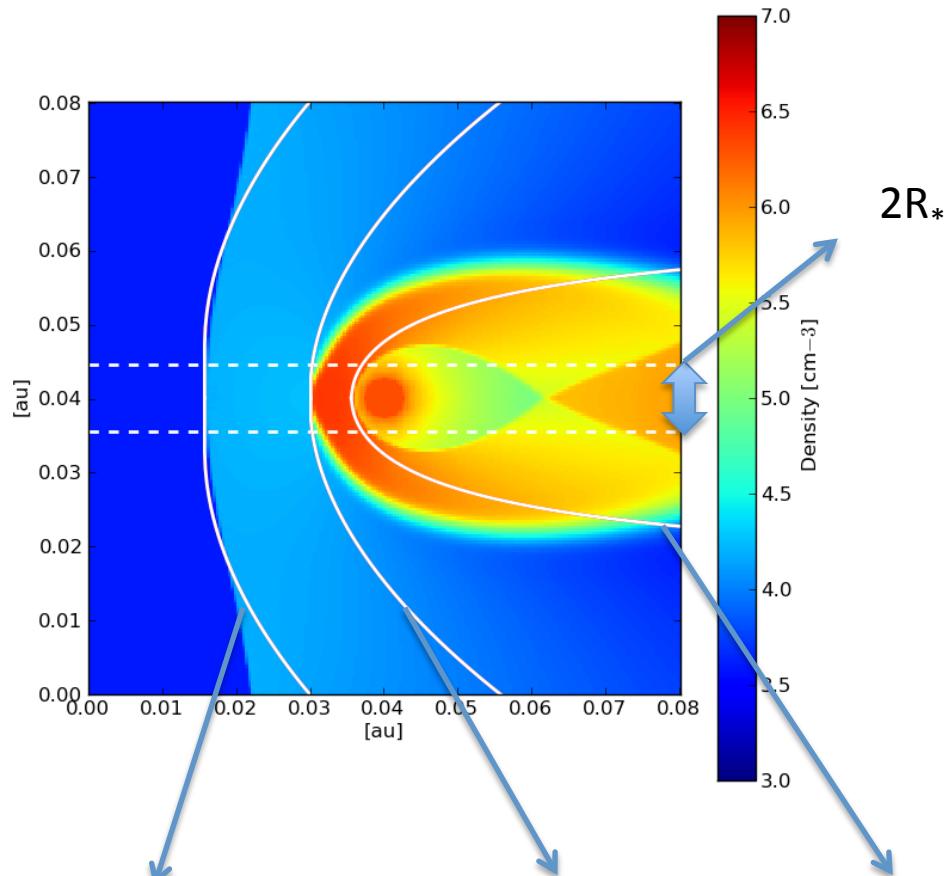
- Opacity for Ly $\alpha$  line:

$$\tau_\nu = 1.041 \times 10^{-14} T_4^{-0.5} N_H e^{-(\nu - \nu_0)^2 / \Delta\nu_{th}^2}$$

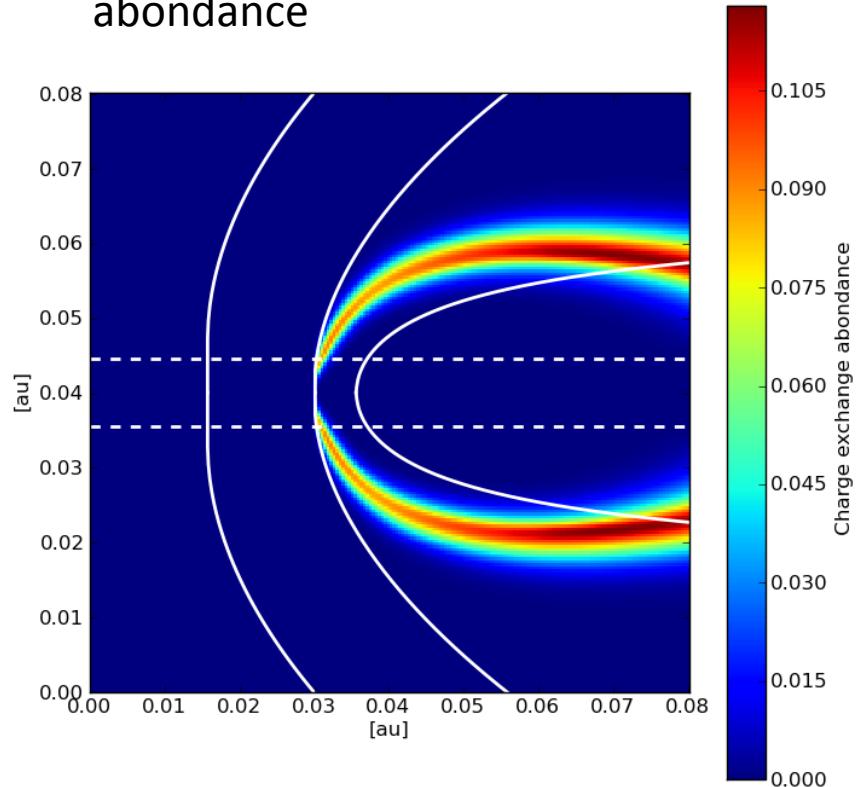
- Doppler shift:  $\nu_0 = (1 + v/c)\nu_{Ly\alpha}$
- Thermal broadening:  $\Delta\nu_{th} = \nu_{Ly\alpha} \sqrt{2k_b T / m_H} / c$

# Results

200x200 2D cartesian  $t=1.2 \times 10^6$  s



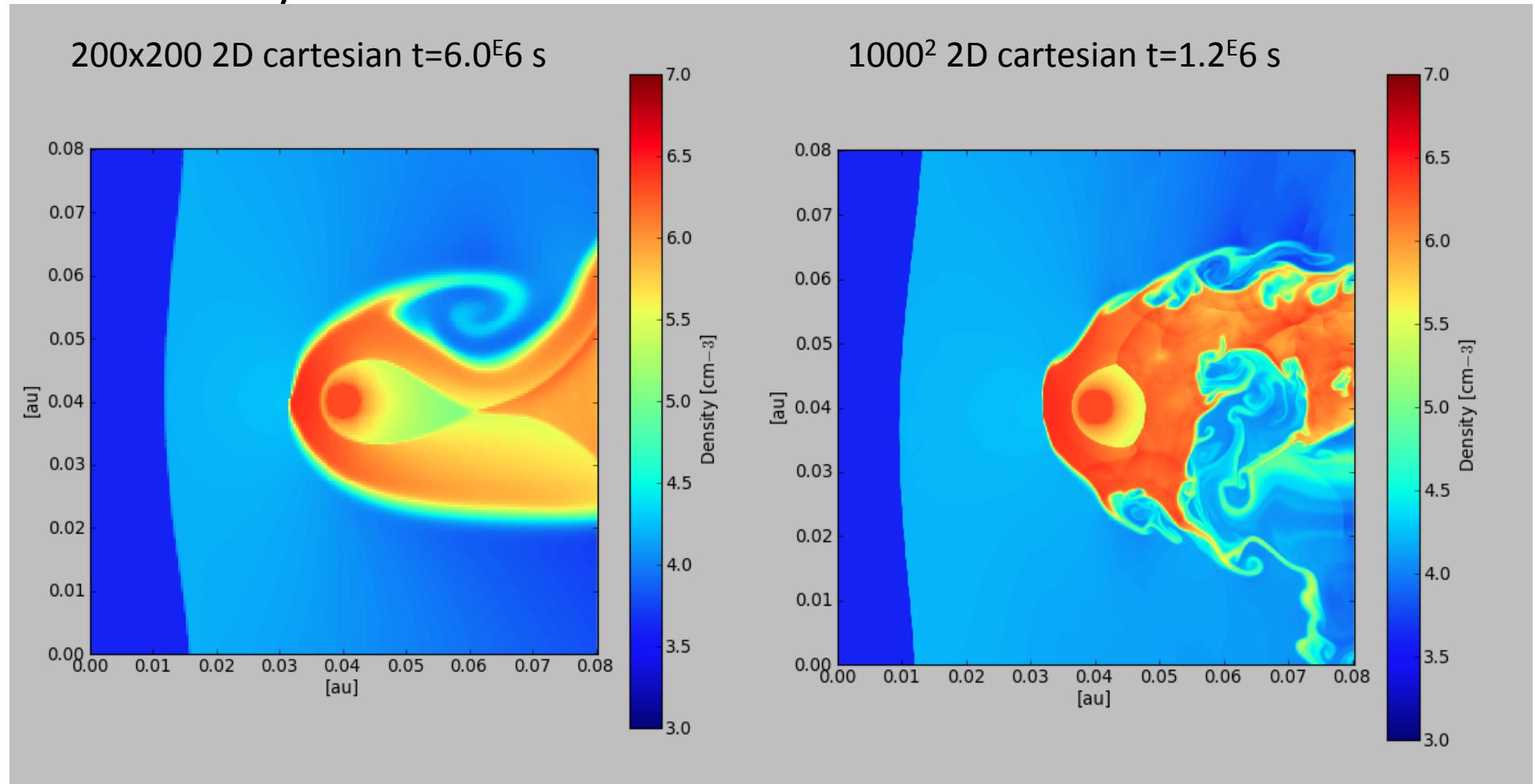
Fast Neutral hydrogen  
abundance



Outer shock      contact discontinuity      inner shock

# Results

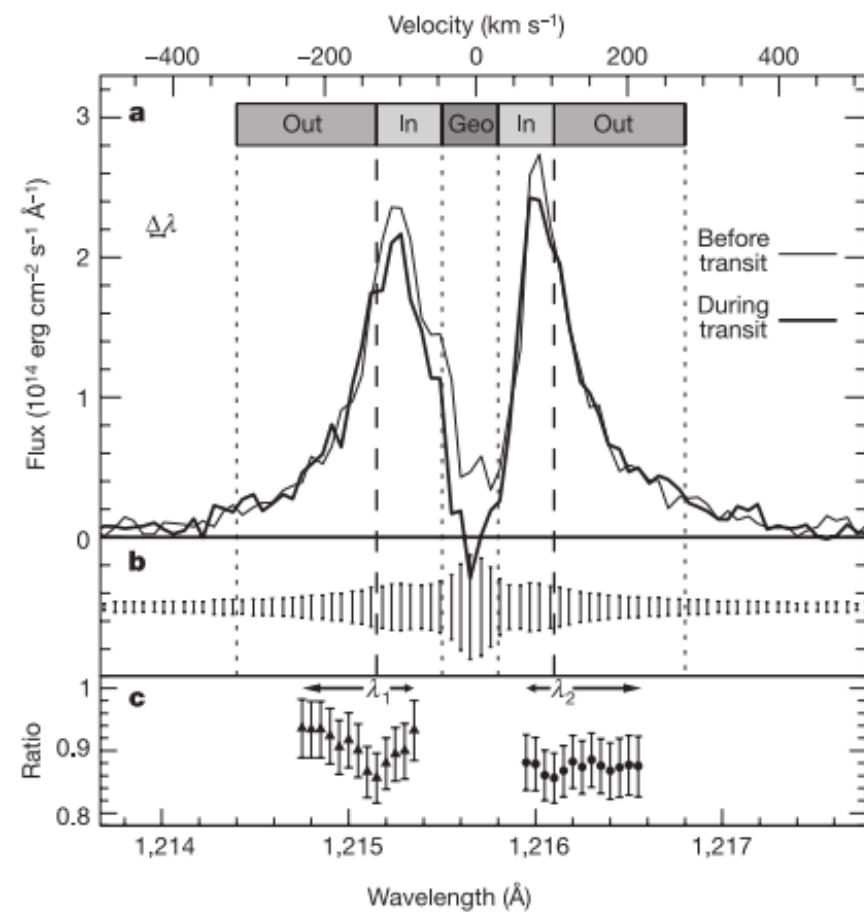
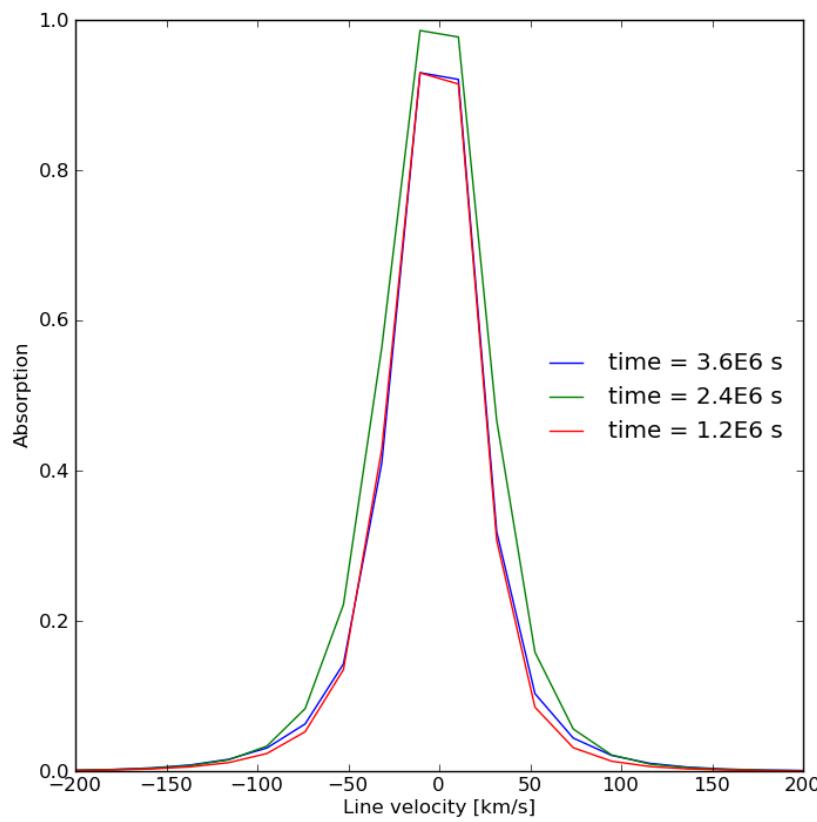
- Steady state ?



# Results

- Absorption spectra

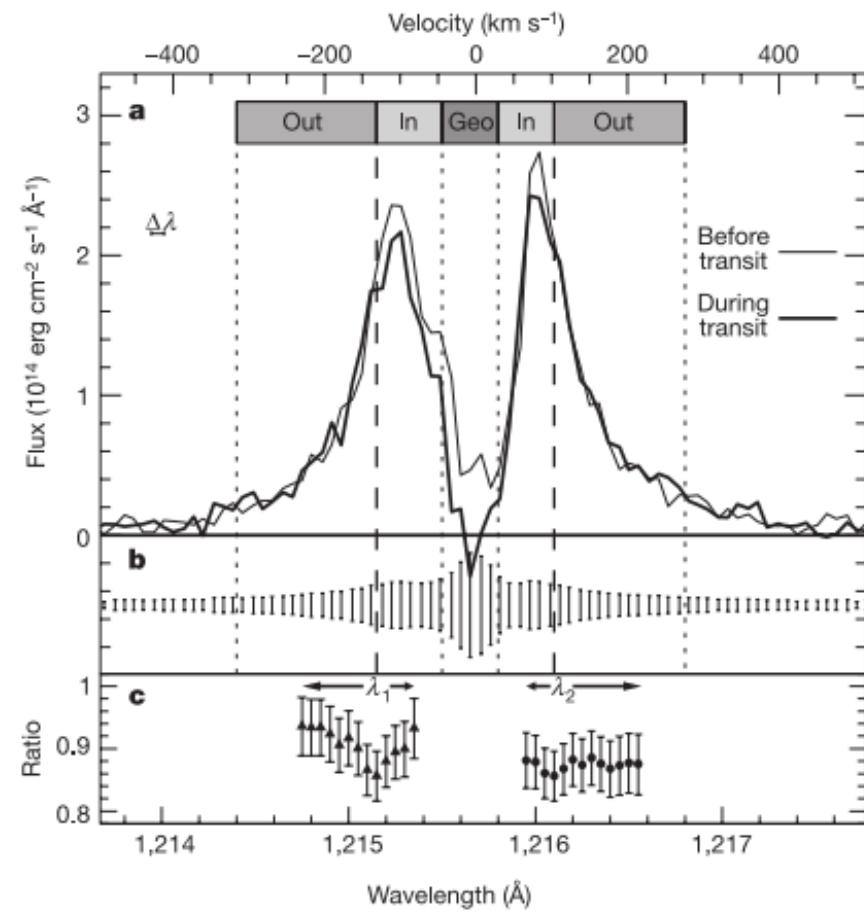
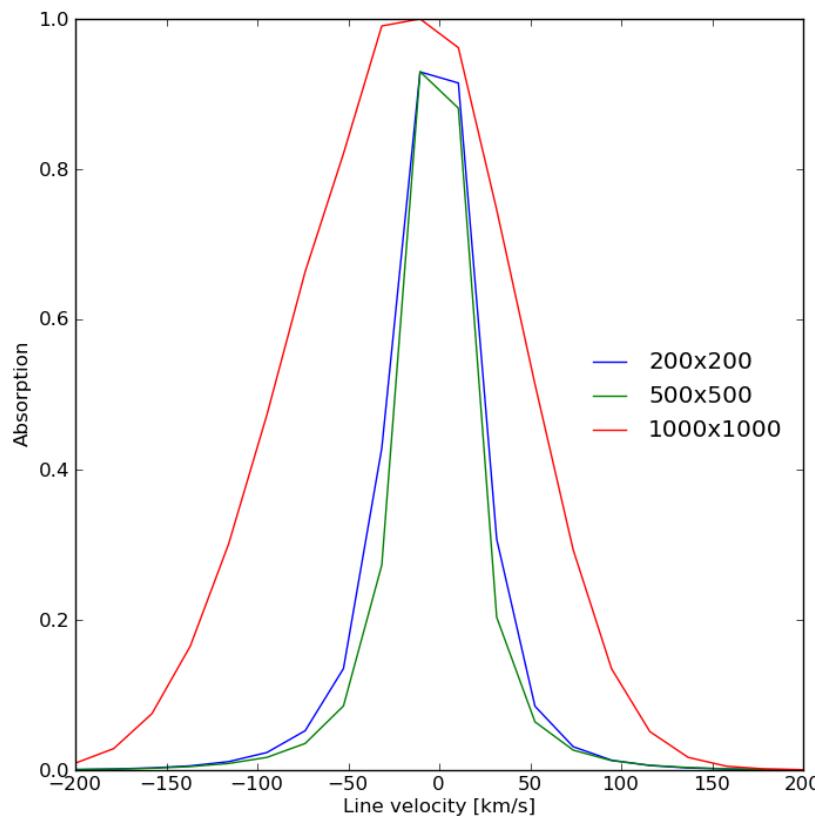
200x200 at different time



# Results

- Absorption spectra

Different resolutions at  $t=1.2 \times 10^6$  s



# Conclusion

- We obtained Ly $\alpha$  absorption spectra due to charge exchange processes in 2D HD simulations
- Upcoming : magnetic field, 3D